

CHAPTER 8

Feedback

8.8 The Stability Problem

8.8.1 Transfer Function of the Feedback Amplifier

Open-loop gain: $A, A(s)$

Loop gain: $A\beta, A(s)\beta(s)$

Close-loop gain: $A_f = \frac{A}{1+A\beta}$ $A_f(s) = \frac{A(s)}{1+A(s)\beta(s)}$ $A_f(j\omega) = \frac{A(j\omega)}{1+A(j\omega)\beta(j\omega)}$

$$L(j\omega) \equiv A(j\omega)\beta(j\omega) = |A(j\omega)\beta(j\omega)|e^{j\phi(\omega)}$$

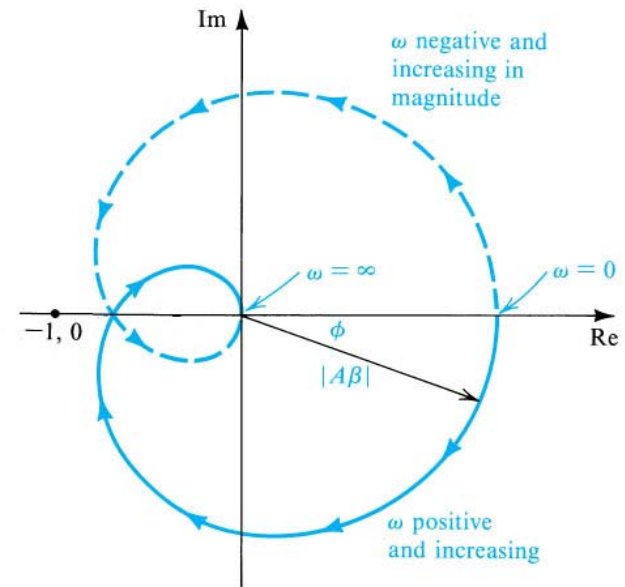
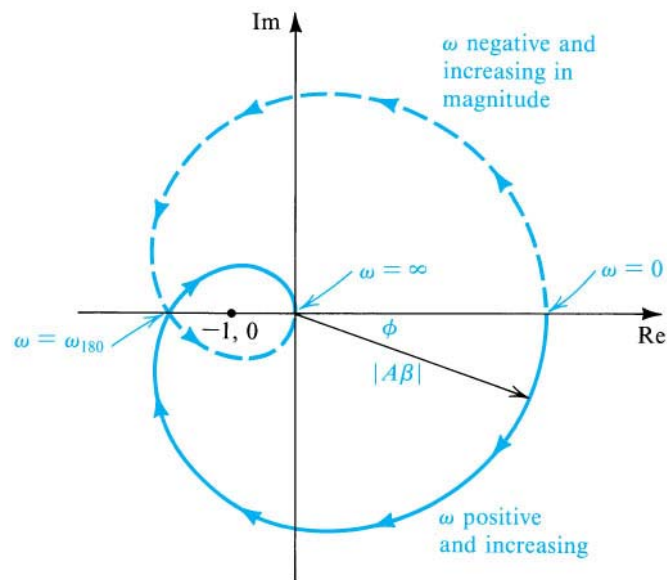
For $\omega = \omega_{180}$ $L(j\omega) \Rightarrow -|A(j\omega)\beta(j\omega)|$

If $|A(j\omega)\beta(j\omega)| < 1$, then $A_f(j\omega) > A(j\omega) \Rightarrow$ stable
Else \Rightarrow unstable

Oscillator: =-1, zero input, infinite output

8.8 The Stability Problem

8.8.2 The Nyquist Plot



If $|A(j\omega)\beta(j\omega)| < 1$, then $A_f(j\omega) > A(j\omega) \Rightarrow$ stable
Else \Rightarrow unstable

8.9 Effect of Feedback on the Amplifier Poles

8.9.3 Amplifier with a single pole

$$A_f(s) = \frac{A(s)}{1 + A(s)\beta(s)}$$

Simplified case

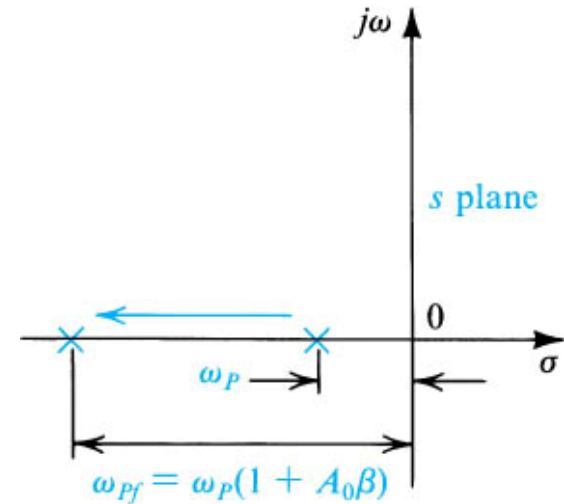
$$A(s) = \frac{A_0}{1 + s/\omega_p}$$

$$A_f(s) = \frac{A_0/(1 + A_0\beta)}{1 + s/\omega_p(1 + A_0\beta)}$$

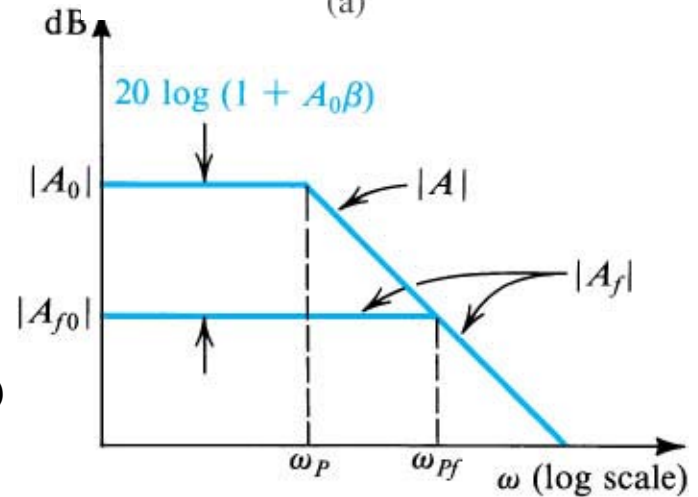
$$\omega_f = \omega_p(1 + A_0\beta)$$

$$\omega \gg \omega_p(1 + A_0\beta)$$

$$A_f(s) \rightarrow \frac{A_0\omega_p}{s} \approx A(s)$$



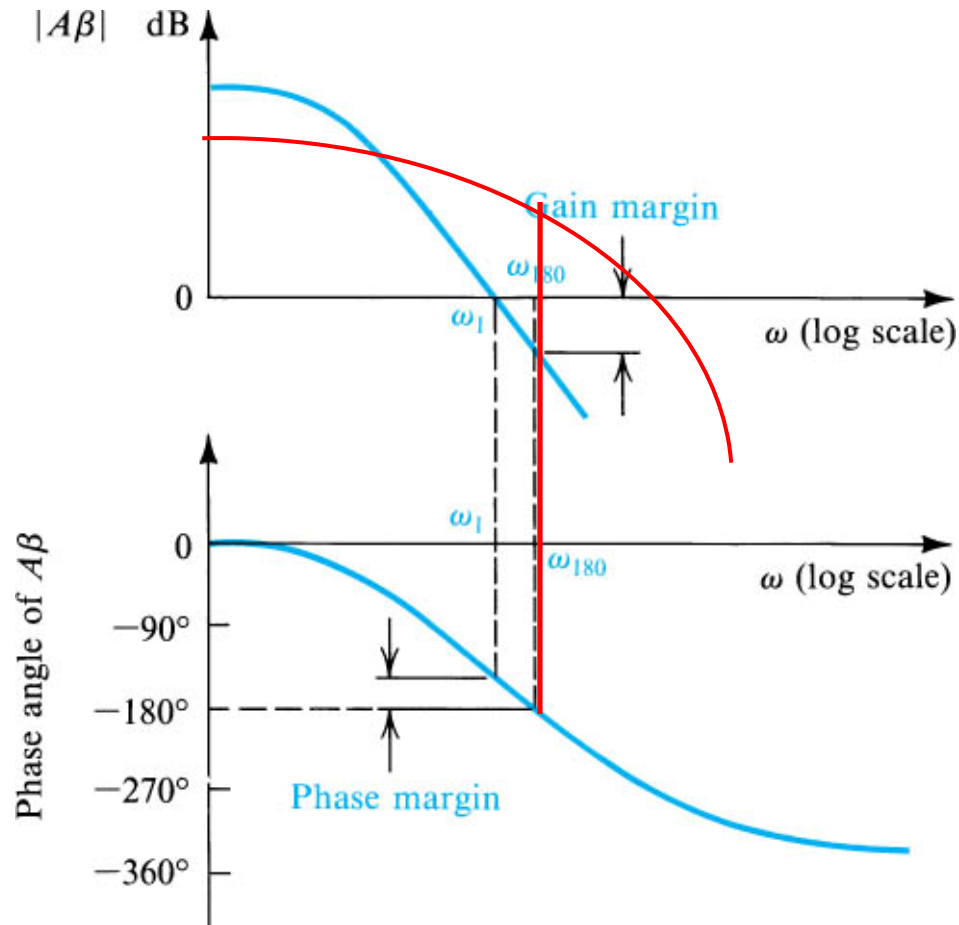
(a)



(b)

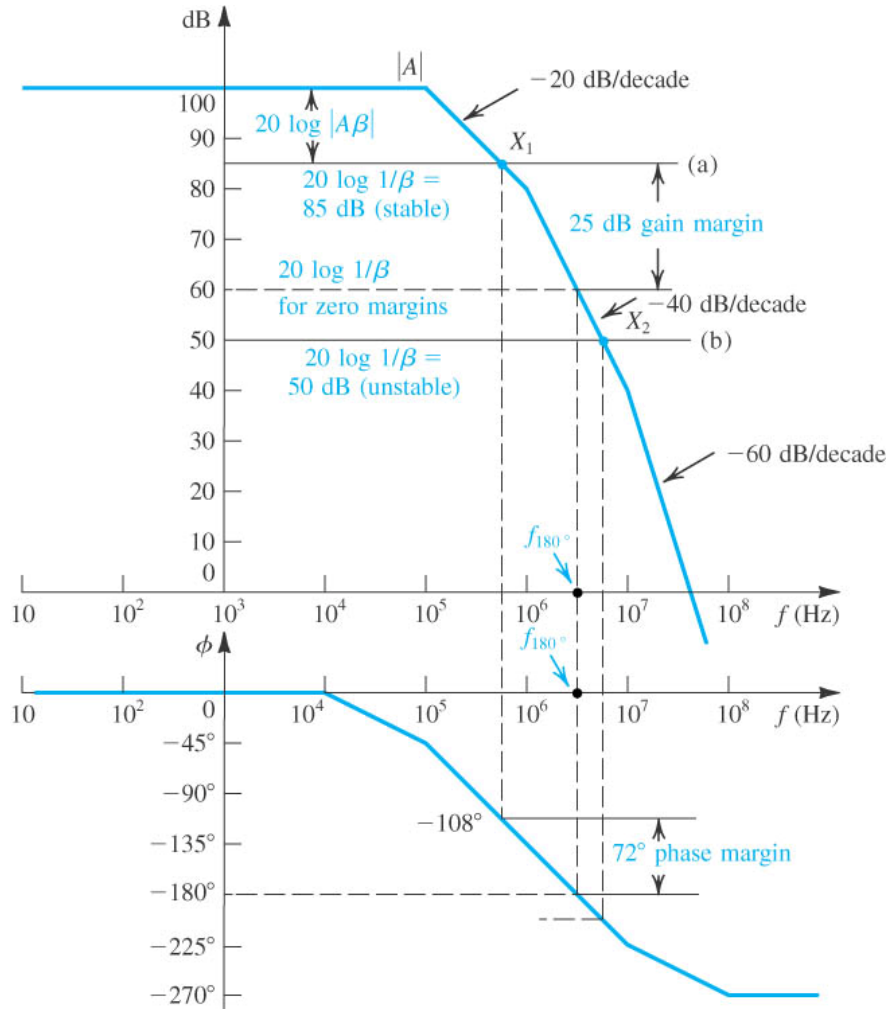
8.10 Stability Study Using Bode Plots

8.10.1 Gain and Phase Margin



8.10 Stability Study Using Bode Plots

8.10.3 An Alternative Approach for Investigating Stability



$$A = \frac{10^5}{(1 + jf/10^5)(1 + jf/10^6)(1 + jf/10^7)}$$

$$A = \frac{10^5}{(1 + jf/10^5)(1 + jf/10^6)(1 + jf/10^7)}$$

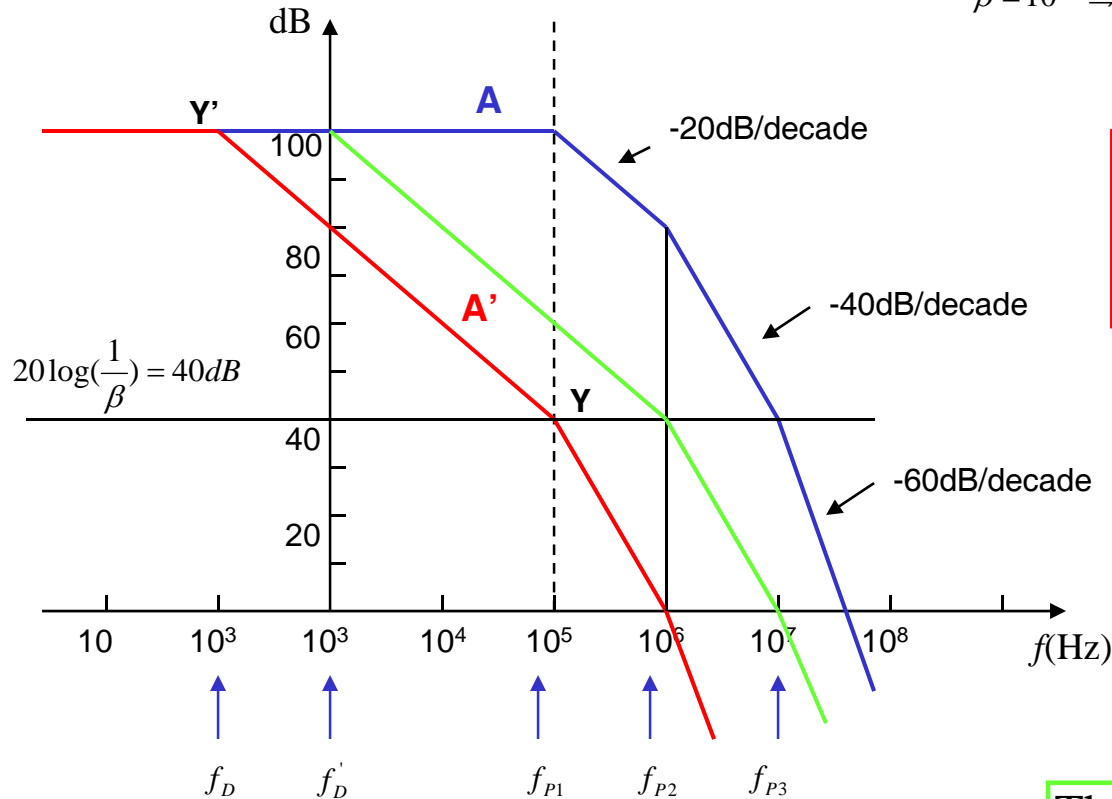
$$|AB| < 1 \Rightarrow 20 \log |A| < 20 \log (1/\beta)$$

The closed-loop amplifier will be stable if the $20 \log(1/\beta)$ line intersects the $20 \log |A|$ curve at a point on the -20-dB/decade segment.

8.11 Frequency Compensation

8.11.1 Theory

$$\beta = 10^{-2} \Rightarrow 20\log\left(\frac{1}{\beta}\right) = 40dB$$

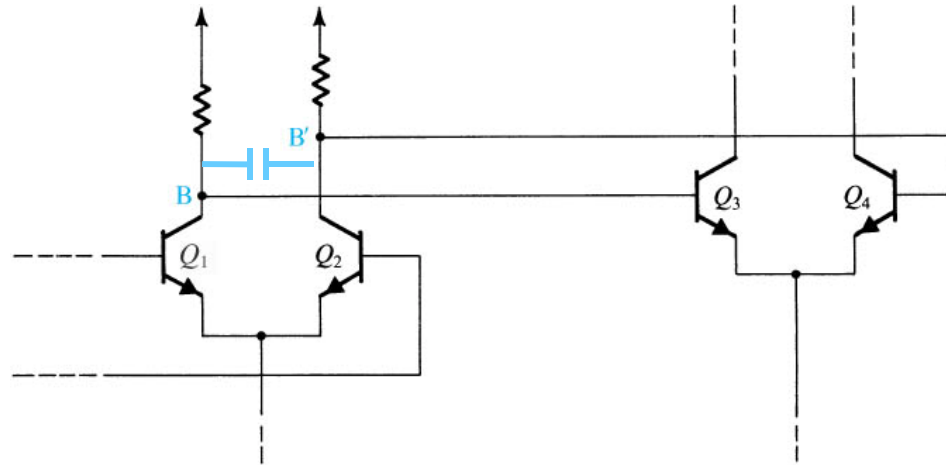


- Four poles
- Simplest
- Reduced the bandwidth

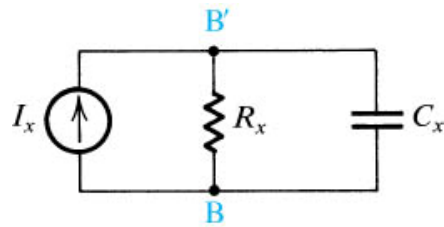
Three poles
 Shift Pole : $f_{p1} \rightarrow f'_D$

8.11 Frequency Compensation

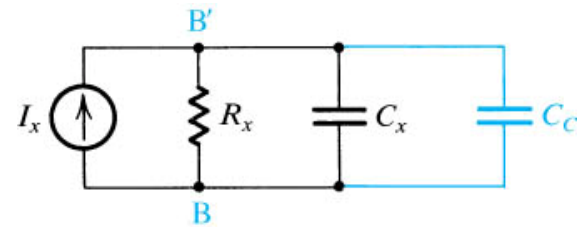
8.11.2 Implementation



(a)



(b)



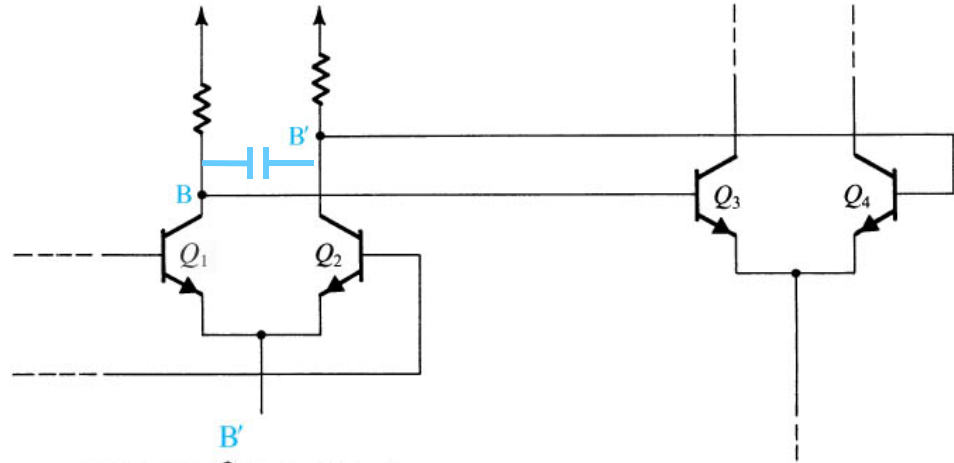
(c)

$$f_{p1} = \frac{1}{2\pi C_x R_x}$$

$$f_{p1} = \frac{1}{2\pi(C_x + C_c)R_x}$$

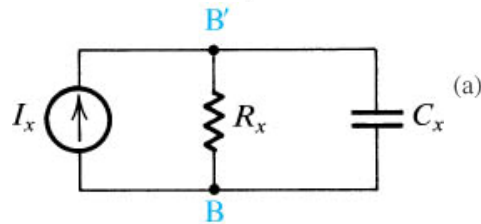
8.11 Frequency Compensation

8.11.2 Implementation



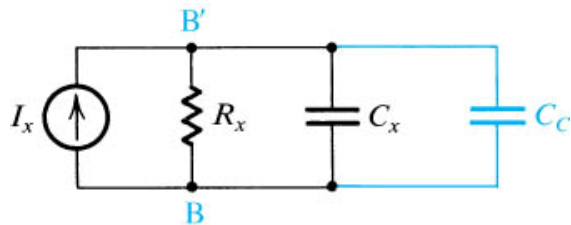
Note:

1. Adding C_c will result in changes in the locations of the other poles
2. C_c is usually large, which is difficult for IC implementation



$$f_{p1} = \frac{1}{2\pi C_x R_x}$$

(b)

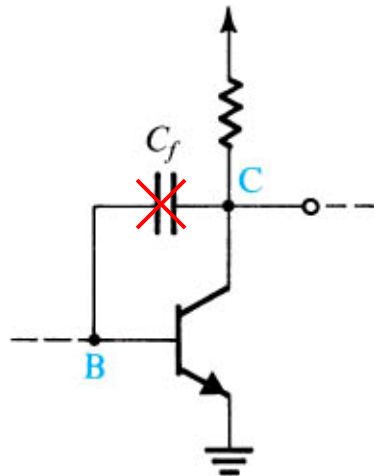


$$f_{p1} = \frac{1}{2\pi(C_x + C_c)R_x}$$

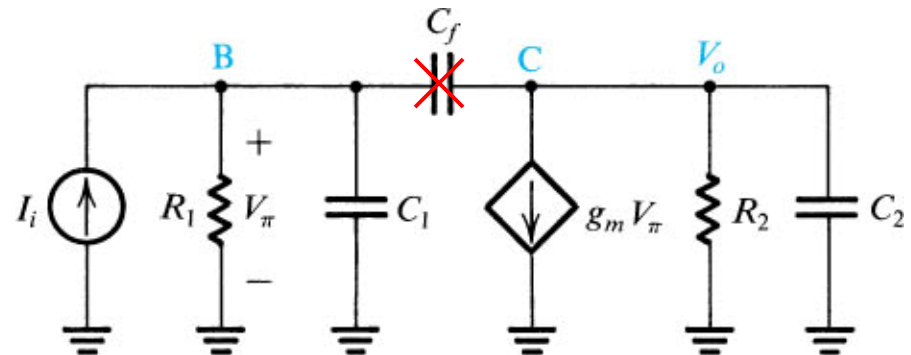
(c)

8.11 Frequency Compensation

8.11.3 Miller Compensation and Pole Splitting



(a)



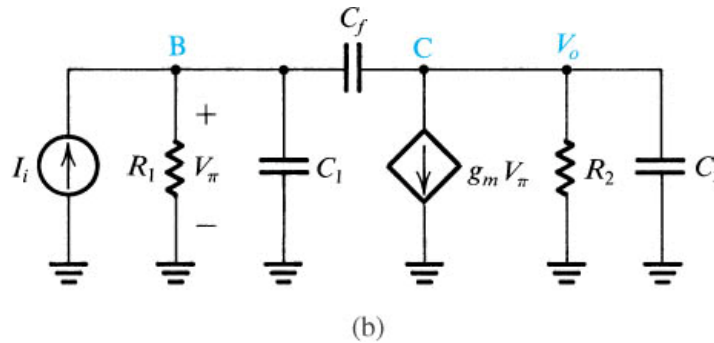
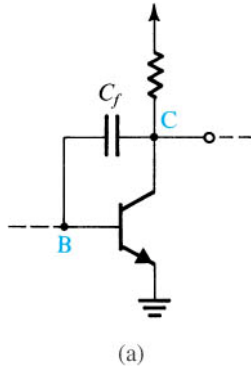
(b)

$$f_{p1} = \frac{1}{2\pi C_1 R_1}$$

$$f_{p2} = \frac{1}{2\pi C_2 R_2}$$

8.11 Frequency Compensation

8.11.3 Miller Compensation and Pole Splitting (cont.)



$$\frac{V_o}{I_i} = \frac{(sC_f - g_m)R_1R_2}{1 + s[C_1R_1 + C_2R_2 + C_f(g_mR_1R_2 + R_1 + R_2)] + s^2[C_1C_2 + C_f(C_1 + C_2)]R_1R_2}$$

$$D(s) = \left(1 + \frac{s}{\omega'_{P1}}\right) \left(1 + \frac{s}{\omega'_{P2}}\right) = 1 + s \left(\frac{1}{\omega'_{P2}} + \frac{1}{\omega'_{P1}}\right) + \frac{s^2}{\omega'_{P1}\omega'_{P2}}$$

$$\omega'_{P1} = \frac{1}{C_1R_1 + C_2R_2 + C_f(g_mR_1R_2 + R_1 + R_2)} \cong \frac{1}{C_f g_m R_1 R_2}$$

$$\omega'_{P2} \cong \frac{g_m C_f}{C_1 C_2 + C_f(C_1 + C_2)}$$

Pole splitting : $C_f \uparrow, \omega'_{P1} \downarrow, \omega'_{P2} \uparrow$

Homework:

8.37, 8.43, 8.47, **Ex-8.14**, 8.70, 8.76, 8.77, 8.79